

# Applications solved by Levenberg-Marquardt Method in implementation of LMDER package by Garbow, Hillstom and Moré

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**Abstract.** In this work we present the results of the Levenberg-Marquardt algorithm in implementation of LMDER package given by Garbow, Hillstom and Moré for solving some real applications considered in the book: "Critica Răspunsei Algoritmilor de Optimizare fără Restricții", chapter 14. The package is in public domain at the address: <http://www.netlib.org/minpack/index.html>.

The purpose of LMDER is to minimize the sum of the squares of  $m$  nonlinear functions in  $n$  variables by a modification of the Levenberg-Marquardt algorithm given by Moré [1978].

## Application Q1. Circuit Design Problem

```
Circuit Design Problem. January 12, 2007
Initial point and Functions values
  1      .70000000000000E+00      .9552504764826E+00
  2      .50000000000000E+00      .3041555430995E+01
  3      .90000000000000E+00      -.4166213167397E+01
  4      .19000000000000E+01      -.2118462145687E+01
  5      .81000000000000E+01      .5636125856655E+01
  6      .81000000000000E+01      .2231397917350E+02
  7      .59000000000000E+01      .2495943321819E+02
  8      .10000000000000E+01      .4218784331013E+02
  9      .19000000000000E+01      -.3200000000000E+00
```

```
-----
OK: iter=      22
LMDER package: Solution of the problem
```

```
  1      .9001161057629E+00      .1834670959801E+00
  2      .4467129934365E+00      .4551467965421E+00
  3      .1006753683178E+01      -.1461477278317E+00
  4      .1974001028530E+01      -.1119427379992E+00
  5      .8015978949713E+01      -.1984811967144E-01
  6      .7989079021508E+01      -.2129287326639E-02
  7      .5090375808511E+01      .5904981885450E-02
  8      .1002067813354E+01      -.7299838599522E-02
  9      .2032419024249E+01      .2438329626292E-01
nfev=      26      njev=      21
```

## Application Q2. (Propan combustion in aer)

```
Propan Combustion in aer Problem. January 12, 2007
Initial point and Functions values
  1      .10000000000000E+02      .10985000000000E+03
```

```

2      .10000000000000E+02      .2095426765244E+03
3      .50000000000000E-01      -.3487418805780E+00
4      .50500000000000E+02      .5098517207139E+04
5      .50000000000000E-01      .2659293083406E+04
-----
OK: iter=      11
LMMDER package: Solution of the problem

1      .3114102265905E-02      -.1387778780781E-16
2      .3459792453121E+02      .00000000000000E+00
3      .6504177869658E-01      .5551115123126E-16
4      .8593780505780E+00      .4218847493576E-14
5      .3695185914805E-01      .2220446049250E-14
nfev=    11      njev=    10

```

### **Application Q3. (Stationar solution of a chemical reactor)**

```

Solution of a chemical reactor. January 12, 2007
Initial point and Functions values
1      .10900000000000E+01      -.35164864000000E+02
2      .10500000000000E+01      -.24030400000000E+00
3      .30500000000000E+01      .36269463700000E+04
4      .99000000000000E+00      -.17799233210000E+04
5      .60500000000000E+01      -.18147127290000E+04
6      .10900000000000E+01      -.71300000000000E+01
-----
OK: iter=      6
LMMDER package: Solution of the problem

1      .9742436189517E+00      .2442490654175E-14
2      .9828290793011E+00      -.2071122610979E-16
3      .5151276209660E-01      -.1048643810675E-10
4      .9356710687406E+00      .5240780032167E-11
5      .9083976760406E-04      .5243194767246E-11
6      .6423809149184E-01      -.2775557561563E-16
nfev=    6      njev=    5

```

### **Application Q4. (Robot Cinematics Problem)**

```

Robot Cinematics Problem. January 12, 2007
Initial point and Functions values
1      .16400000000000E+00      .26823690400000E-02
2      -.98000000000000E+00      -.98180480000000E-02
3      -.94000000000000E+00      .99542820000000E-01
4      -.32000000000000E+00      .17588000000000E-02
5      -.99000000000000E+00      -.12704000000000E-01
6      -.50000000000000E-01      -.14000000000000E-01
7      .41000000000000E+00      -.17400000000000E-01
8      -.91000000000000E+00      -.38000000000000E-02
-----
OK: iter=      5
LMMDER package: Solution of the problem

1      .1644316658543E+00      .00000000000000E+00
2      -.9863884768510E+00      .00000000000000E+00
3      -.9470636915416E+00      .2602085213965E-17
4      -.3210457353143E+00      .00000000000000E+00
5      -.9982331646551E+00      -.1110223024625E-15
6      .5941842292353E-01      .2220446049250E-15
7      .4110331567472E+00      .00000000000000E+00
8      -.9116203947118E+00      .00000000000000E+00
nfev=    5      njev=    4

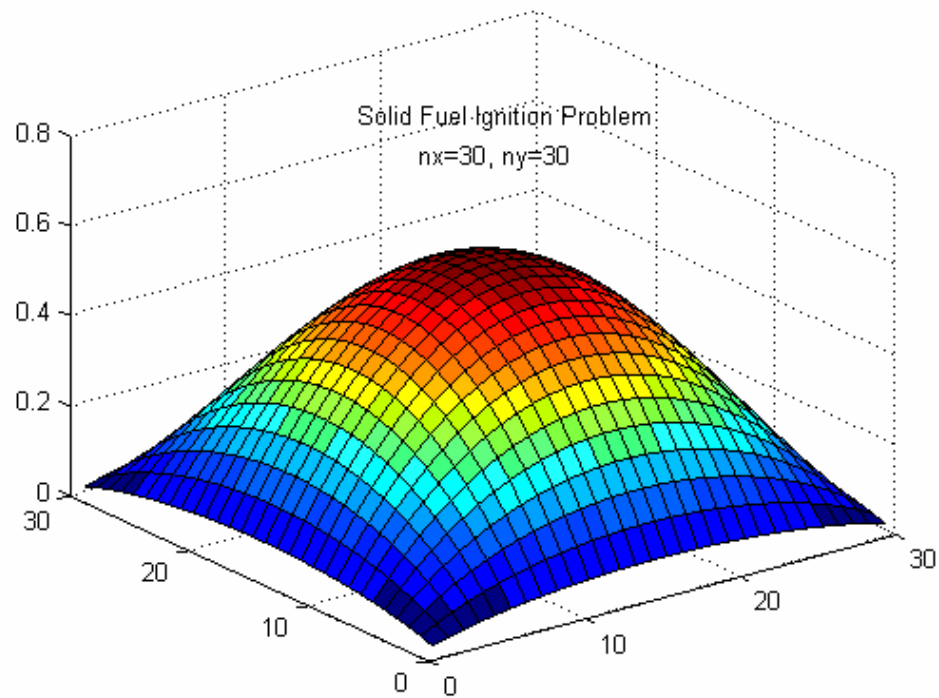
```

### **Application Q5. (Solid Fuel Ignition Problem)**

Solid Fuel Ignition Problem. January 12, 2007

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OK: iter= 5  
LMMDER package: Solution of the problem  
nfev= 5 njev= 4



**Fig. Q5.** Solid fuel ignition. Bratu Problem.

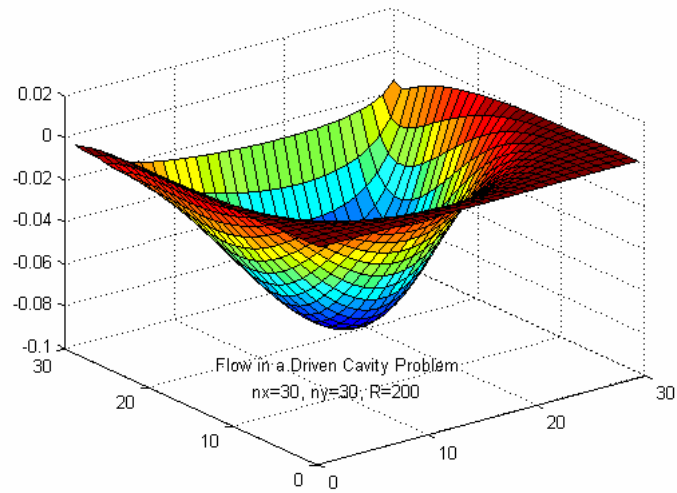
### **Application Q6. (Flow in a Driven Cavity Problem)**

For: **nx = 30, ny = 30, R=200** we get:

Flow in a Driven Cavity Problem. January 12, 2007

---

OK: iter= 6  
LMMDER package: Solution of the problem  
nfev= 6 njev= 5



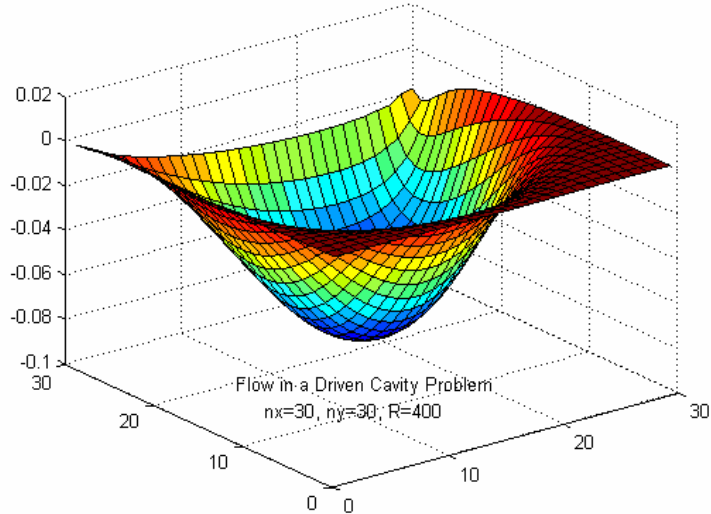
**Fig. Q6a.** Solution of the problem.  $R=200$ .

For:  $nx = 30$ ,  $ny = 30$ ,  $R=400$ , we get:

Flow in a Driven Cavity Problem. January 12, 2007

-----  
OK: iter= 7  
LMMDER package: Solution of the problem

nfev= 7 njev= 6



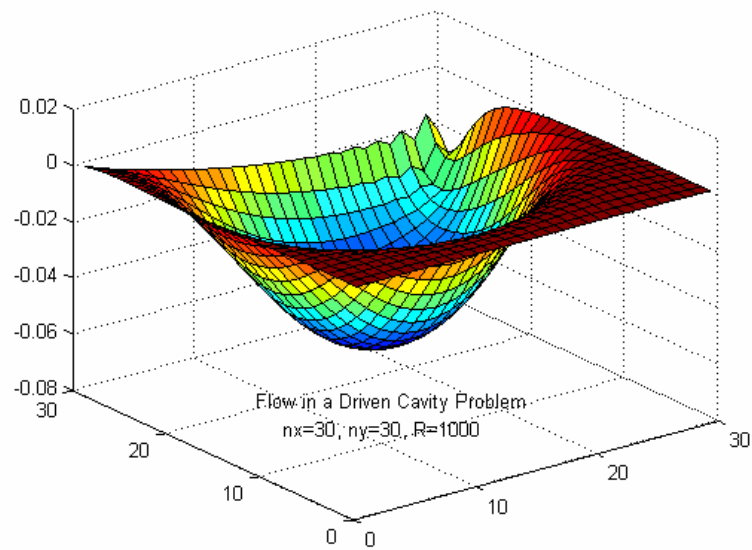
**Fig. Q6b.** Solution of the problem.  $R=400$ .

For:  $nx = 30$ ,  $ny = 30$ ,  $R=1000$  we get:

Flow in a Driven Cavity Problem. January 12, 2007

-----  
OK: iter= 11  
LMMDER package: Solution of the problem

nfev= 13 njev= 10



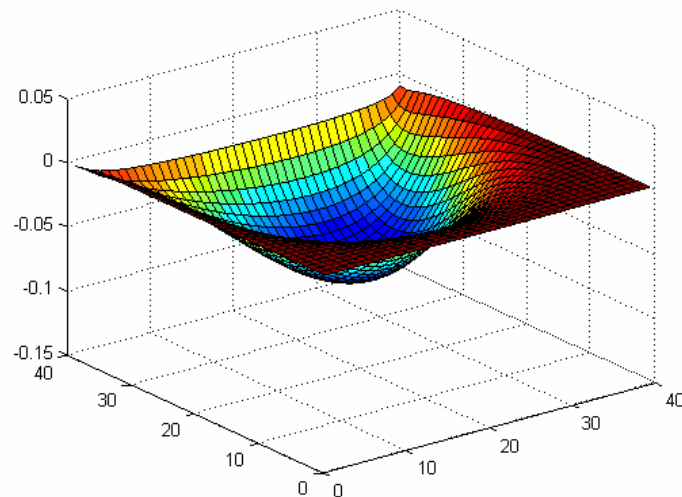
**Fig. Q6c.** Solution of the problem.  $R=1000$ .

For:  $nx = 40, ny = 40, R=200$  we get:

Flow in a Driven Cavity Problem. January 15, 2007

```
-----
OK: iter=      6
LMMDER package: Solution of the problem

nfev=      6   njev=      5
```



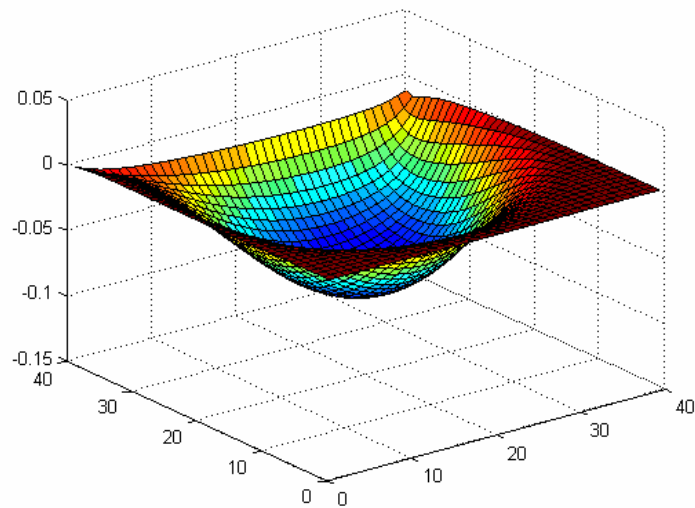
**Fig. Q6d.** Solution of the problem.  $R=200$ .

For:  $nx = 40, ny = 40, R=400$  we get:

Flow in a Driven Cavity Problem. January 15, 2007

```
-----
OK: iter=      7
LMMDER package: Solution of the problem

nfev=      7   njev=      6
```



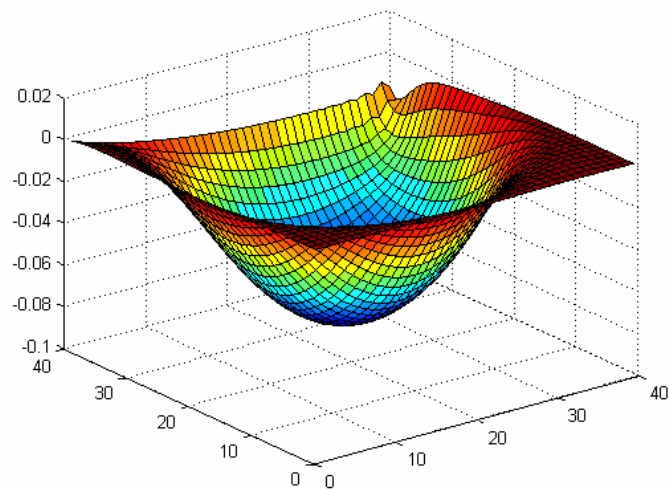
**Fig. Q6e.** Solution of the problem.  $R=400$ .

For:  $nx = 40$ ,  $ny = 40$ ,  $R=1000$  we get:

Flow in a Driven Cavity Problem. January 15, 2007

```
-----
      OK: iter=      11
      LMMDER package: Solution of the problem

      nfev=      11   njev=      10
```



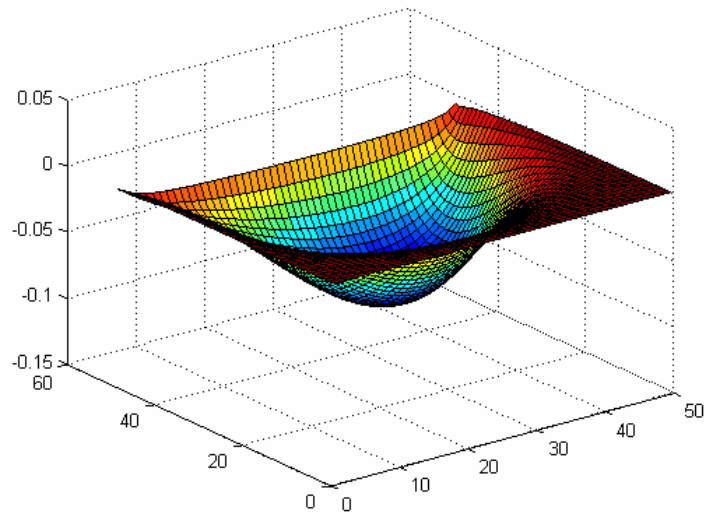
**Fig. Q6f.** Solution of the problem.  $R=1000$ .

For  $nx = 50$ ,  $ny = 50$ ,  $R=200$  we get:

Flow in a Driven Cavity Problem. January 15, 2007

```
-----
      OK: iter=       6
      LMMDER package: Solution of the problem

      nfev=       6   njev=       5
```

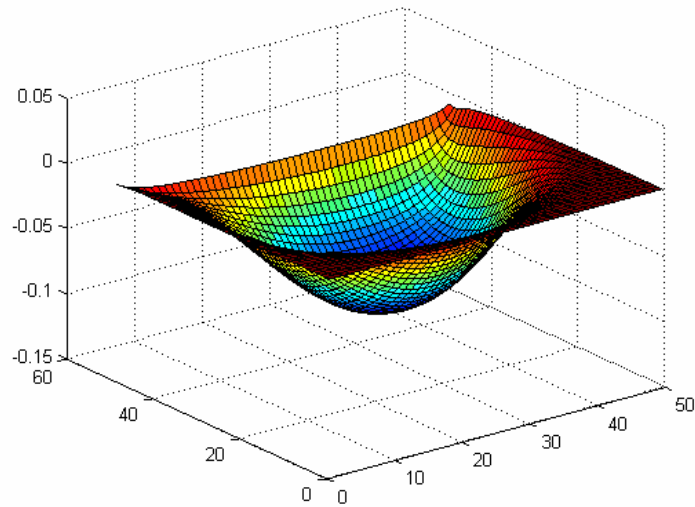


**Fig. Q6g.** Solution of the problem.  $R=200$ .

For  $nx = 50, ny = 50, R=400$  we get:

Flow in a Driven Cavity Problem. January 15, 2007

```
-----
      OK: iter=      7
      LMMDER package: Solution of the problem
      nfev=      7   njev=      6
```

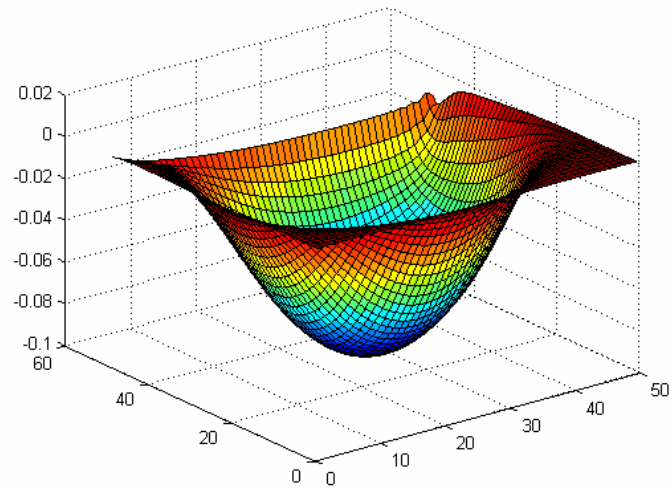


**Fig. Q6h.** Solution of the problem.  $R=400$ .

For  $nx = 50, ny = 50, R=1000$  we get:

Flow in a Driven Cavity Problem. January 15, 2007

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      OK: iter=      8
      LMMDER package: Solution of the problem
      nfev=      8   njev=      7
```



**Fig. Q6i.** Solution of the problem.  $R=1000$ .

**January 15, 2007**